MAPS: Machine-based Automatic Phone Surveillance

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ABSTRACT

Exploring potential threats to electronic media has been an area of active interest in computer security for the purpose of prevention of these threats. We examine a threat scenario that involves eavesdropping on phones with virtual keypads, a class of phones becoming increasingly popular by the day. We explore an approach to automatically recover the text that was typed by a person on his phone, based solely on a video of this typing activity by observing the phone directly, or by observing a reflection of the phone in the user's glasses or even his eyes. Our experiments were conducted on two popular smart phones, the iPhone and the Nexus One; the same approach can be extended for surveillance on a variety of phones and devices with virtual keypads.

KEYWORDS: Surveillance, Eavesdropping, Data security, Phone security

1 INTRODUCTION

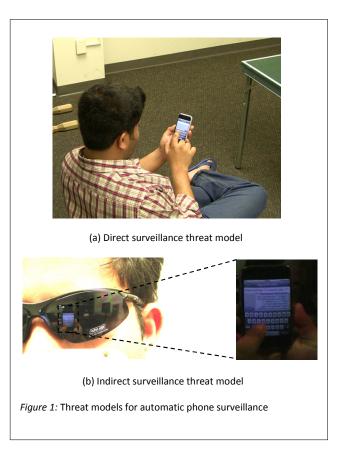
Bob, on his way to work, is sitting on a bus typing an email on his smart phone. Alice, sitting right across him, records a video of the reflection of Bob's typing activity on his glasses. She records this video using her cell phone camera; so no one around is suspicious. Meanwhile, a program on Alice's phone uses this video to automatically retrieve the complete text of what Bob was typing.

At first, the scenario above looks like a scene from one of the numerous unrealistic James Bond or CSI movies. However, after you have read this paper, we are sure that you would believe that this scene could be real and could happen to any of us in the near future. In this paper, we explore the feasibility of threats similar to the one described above. We apply state-of-the-art tools in computer vision to examine how real this threat is and whether it can be carried out using cheap equipments that cost no more than a few hundred dollars.

Recently, there has been a flood of smart phones in the market. Sale statistics on the internet show that around 300 million smart phones were sold in the year 2010 [12]. More than 50 million units of iPhone were sold within the last two years [10], and more than 100,000 units of the Nexus One were sold within the first three months of its release in 2010 [11]. The increasing popularity of these internet-enabled smart phones has resulted in these phones being used by a large number of people for the exchange of various types of information. Apart from making calls and sending text messages, they are used for sending emails, sharing photographs downloading audio/video media, among a lot of other things. There are predictions that mobile phones would become the primary personal computing devices in the near future [9], replacing laptops and notebook computers.

With the growing popularity of mobile devices in the last few years, attacks targeting them are also surging [13]. Network intrusion attacks and their defenses have received a considerable amount of attention in the recent past. Back in 2004, Guo et al. [14] and Wang

et al. [15] had pointed out probable attacks in smart phone networks and suggested solutions. Since then, there has been a lot of research in such threats. [13], [23] and [24] are some recent papers which suggest different approaches for privacy monitoring in data entering and leaving smart phones.



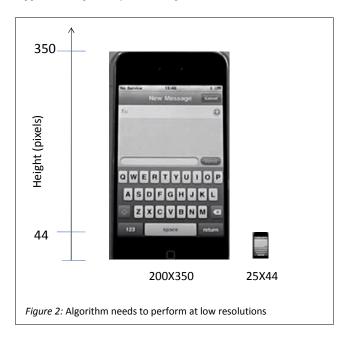
While cryptographic mechanisms have been effective in preventing different types of eavesdropping on phones, they cannot protect the physical environment of the victim. So far, there has not been any extensive study on how camera-based surveillance can be used to threaten the privacy of a phone user. Today's world is full of surveillance cameras ubiquitously present in all public places. Additionally, pocket camcorders, cell phone cameras, and other small sized video capture devices are getting more powerful as well as cheaper by the day. Spying on people has always been an effective way of information retrieval and smart phone users could soon become targets. Hence the threat that we attempt to study in this paper is very relevant in the current scenario. Figure 1 shows the two types of threat scenarios that we examine; the first one (which we call *direct surveillance*) happens when the camera has a direct view of the typing activity, and the second one (indirect surveillance) happens when the camera records a reflection of this activity on the victims glasses, or his eyes, or some other reflective

surface nearby, like a window pane, a teapot etc. Of course, an automated tool, such as the one that we have designed, is required in the case of long-lasting surveillance procedures or long user activity.

Automatic surveillance on a phone is a hard problem that poses several challenges. One particular issue is that without the use of expensive and sophisticated cameras, it is not possible to have a resolution high enough to read what is displayed on phone display screen. As a result, we cannot use optical character recognition methods [16]. We approached the problem by an analysis of hand gestures and other movements on the touch-screen of the phone.

Motion analysis in our threat scenario is complicated because of various reasons. One of the reasons is that there are two types of motion to be dealt with: the motion of the user's fingers on the touch-screen of the phone, as well as the overall motion of the phone itself. The latter is a distraction for us; we are only interested in what movement takes place on the touch-screen, not the phone movement when the user is typing on it. This is a relative advantage of using motion analysis for surveillance on a computer keyboard [4], as the keyboard stays stationary when the user is typing on it.

The phone screen is a relatively small object when compared to the size of a user's hands; a large part of the phone is occluded by the user's fingers when he is typing. This occlusion poses challenges when standard computer vision techniques are applied for tracking, recognition and registration of the phone in the video. The wide variations in the viewing angle of the phone in different videos also pose a challenge in phone tracking. Depending on the scenario, it might be extremely difficult to get a good frontal view of the phone screen; in a video without a good view, motion analysis is an even bigger challenge than phone recognition.



One of the foremost challenges in camera-based automatic phone surveillance is the resolution at which the algorithm is required to perform for the threat to be real. As explained in Appendix-I [Section 8], the maximum resolution of an object in an image is directly proportional to the size of the object and the diameter of the camera lens. It is also inversely proportional to the distance of the object from the camera. While it is possible to capture a very high resolution image of the phone by using a large telescope, it makes the security threat unreal as it would be hard to spy on a person with a huge telescope right in front of her. It would also be very expensive and is not the kind of threat that we are interested in. Limitations in the size of the camera lens in cheap digital cameras, pocket camcorders or mobile phone cameras result in limitations in the resolution of the images that can be captured by them. Formulae in Appendix-I predict that our approach needs to perform at far lower resolutions than what is required for the human eye. Figure 2 shows two images, the first of which is an image in which the iPhone has a resolution of 200X350 pixels and in the second one the iPhone has a resolution of 25X44 pixels. Our algorithm has produced very promising results for a surveillance video at the resolution of the second image; for effective indirect surveillance using a cell phone camera, we need the ability to perform at even lower resolution than that.

We are also very interested in recovering data from reflections. We have shown promising results for automatic surveillance from a video of the reflection of the victim's typing activity on his sunglasses. Figure 1(b) shows our experimental setup for this case. One of the obvious challenges in recovering data from reflections is because of the size of the object under surveillance. While the size of an iPhone is about 11.5 cm X 6 cm [17]; the size of this phone's reflection on a pair of sunglasses would be about 1.07 cm X 0.57 cm [Section 8], which is around a tenth of the original object size; the size of this phone's reflection on a human eye would be about 1.6 mm X 0.86 mm [Section 8], which is around a hundredth of the object size! Direct surveillance itself causes a low-resolutionchallenge for our algorithm; it is obvious that indirect surveillance, where the object being monitored is much smaller, poses an even harder low-resolution-challenge. Additionally, depending on the surface where the reflection takes place, there might be a need for distortion correction of the reflected image. Distortion correction in reflected images is in itself a major research topic in computer vision. Nishino and Nayar [18] have done seminal work focused on rectifying images that capture reflections of the surrounding environment on the human eye. We have not addressed this issue yet but as we apply our algorithm to eye reflections in the near future, we would need to do so.

The current contributions of our work are:

- We show that it is possible to automatically reconstruct the text being typed by a user on a virtual keypad phone by analyzing solely the video stream of the typing activity.
- We have developed a robust method for tracking the phone as well as analyzing the user's motion by using state-of-the-art techniques in computer vision.
- We have examined the threat of automatic phone surveillance via monitoring of the reflection of the phone in the user's glasses.

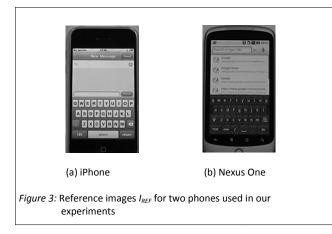
The remainder of this paper is organized as follows. In Section 2 we talk about some previous work that are related to our topic, and which have inspired us in several ways. Section 3 explains the details of our method in several sub-sections. In Section 4 we present some of our results. In Section 5, we give a discussion of how real this threat is and what kind of optical instruments are required to carry out this threat. In Section 6, we conclude and mention some of the steps that we are taking in the future.

2 RELATED WORK

Backes et al.[1] have presented a novel eavesdropping technique for spying at a distance on data displayed on an LCD monitor by capturing images from reflections in various common objects like eye-glasses, teapots, spoons, and even the human eye balls. They present results of capturing data from distances ranging from 5m to 30m, with equipments that include high quality SLR cameras, low cost telescopes as well as very expensive and large size telescopes. Balzarotti et al [4] have presented a novel approach for eavesdropping on keyboard input from surveillance videos. Their approach assumes that the keyboard is placed on a flat table, the user's hands have restricted movement, the camera has a clear overhead view of the typing activity, and that the keyboard does not move when the user is typing. While these are all reasonable assumptions for keyboard surveillance, none of them hold true in the case of phone surveillance. While typing on the phone, the user has complete freedom of moving the phone as well as moving his hands. It is also not always feasible to have a clear view of the typing activity because of occlusion of the phone by the user's hands, face and shoulders. Also, even when a clear view is present a large part of the phone is still occluded by the user's fingers when he is typing on it. Hence, while the approach presented by Balzarotti et al has provided good results for keyboard surveillance, it cannot be directly extended to phone surveillance.

3 APPROACH

The goal of our work is to automatically reconstruct the text typed by a user by analyzing a video recording of the typing session. Figure 4 is a flowchart of our approach. The inputs to our method are the surveillance video and some prior information about the phone being tracked, namely, the keypad layout and a reference image of that phone. Both these facts can be easily obtained from an online user manual of the phone. Figure 3 shows reference images for two of the phones we used in our experiments.

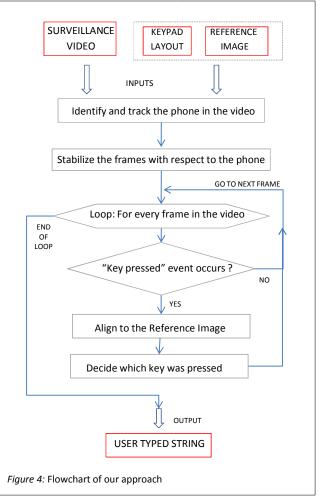


The reference image is used by our algorithm to track and identify the location of the phone in the surveillance video. Our tracking algorithm, the details of which are in Section 3.2, gives information about the location as well as orientation of the phone in any particular frame of the video. Given the location of the phone in a particular frame, we would then like to focus our attention on that particular area of the frame.

The tracking step in our method is followed by a stabilization step [Section 3.3], in which we align the image of the phone in successive frames of the input video. As we shall explain later, this helps us to nullify the overall motion of the phone and concentrate on the movement of the users fingers on the virtual keypad.

Our next task is to detect "key pressed" events across the video [Section 3.4]. A "key pressed" event is one in which the user has typed a single character on his keypad. There is one particular

feature in most smart phones (with a virtual keypad) that tremendously helps us in detecting such events. This feature is that whenever a user presses a particular key, that key pops up on the phone screen. For example [Figure 7], when the user presses the letter 'T', a big 'T' pops up somewhere on the phone screen to let the user know what he has just typed. Using change detection



techniques coupled with the information provided by our tracking algorithm, we are able to detect such "key pressed" events.

For every frame in the video, the method described in Section 3.4 answers the question, "Was a key pressed by the user in this frame?" If the answer to the previous question is affirmative, our task then is to predict which key was pressed by the user in this particular event. Determination of which key was pressed requires an alignment of the phone in this video frame to the *Reference Image* of the phone. Our algorithm [Section 3.5] makes use of the output of the previous steps, as well as the prior knowledge about the phone keypad layout to provide this analysis [Section 3.5].

We have now identified the individual characters that were pressed by the user during the "key pressed" events in the video. Because of various challenges involved in the different stages of our approach, it is extremely hard to produce a 100% correct output, i.e, the output of our approach needs to undergo some additional text processing to produce higher accuracy results. We are still in the process of exploring probabilistic text processing tools to assist us and the results reported in this paper does not include that step.

3.1 Background

This section provides an introduction to some of the computer vision tools used in our approach. *SIFT* [3] is a powerful feature descriptor that we use for feature tracking in various stages of our method. The *SIFT descriptor* of a region consists of a histogram of gradients in that region. SIFT descriptors are widely used because they associate to each region a signature which identifies their appearance in a compact and robust way. They are consistent with considerable variations of the illumination, viewpoint and other viewing conditions [25]. *Maximally Stable Extremal Regions (MSERs)* [2] are regions in an image that are either brighter or darker than their surroundings. These regions are stable across a range of thresholds of the intensity functions. We use an *MSER* detector in our tracking process to detect regions on the phone that are repeatable across changes in illumination, as well as changes in viewpoint.

A *homography* is a projective transformation that relates a planar object in two different views. The phone screen in one image is related to the same screen in another image by a homography. *Affine normalization* is the process of converting elliptical regions in an image to circles so that these can be matched with other regions which are related to them by an affine transformation. *RANSAC*, which stands for Random Sample Consensus [6] is a widely used method in computer vision for robust estimation of models from data. The method essentially uses random samples to construct a model and then selects the model which has the highest consensus from all other samples. We use RANSAC to estimate a homography between two different views of the same planar object.

3.2 Phone Identification, Tracking and Registration

Determining the location of the phone in the video is extremely helpful to focus our analysis on the object of interest. In any frame in the surveillance video, our tracking algorithm locates the phone by matching areas on the phone in the reference image [Figure 3] to areas in the surveillance image. The reason we chose an area feature detector over widely-used point detectors like Harris Corners [5] was because most of the features returned by point detectors happen to lie in the keypad region of the phone, which is often occluded by the user's hands or fingers. Because of the occlusions, they tend to return fewer relevant features than what is required by our matching algorithm. Moreover, a phone has several distinct regions like the keys, the phone screen etc. which are picked up by the MSER detector with good consistency over a considerable variation of illumination as well as viewing angles. We also observed that the keys on the virtual keypad of the phone are regions of a particular type which are similar in appearance to each other but very different from non-key regions. Hence it is easier to detect the keys on the phone.

Algorithm 1 gives an outline of our tracking approach. We start by detecting MSER regions in the reference phone image, and selecting some regions which are repeatable across different surveillance scenarios. Let us call them the *distinguished regions* D_{ref} . These *distinguished regions* [Figure 4] consist of keys, the phone screen, and some other regions which are frequently detected in different videos. Note that the selection of D_{ref} needs to be done only once for every type of phone that we want to detect. For example, if we select D_{ref} for an iPhone, it can be used for all surveillance videos that track an iPhone.

The surveillance video can be represented by a sequence of frames or images { $I_1, I_2 \dots I_M$ } extracted from the video at times { $t_1, t_2 \dots t_M$ }. For every image I_k in this sequence, we match MSERs detected in this image to the distinguished regions D_{ref} . We represent MSER regions by their SIFT descriptors. SIFT descriptors are very suitable for our case as the image of the phone undergoes a lot of variation in lighting conditions as well as viewing angles in

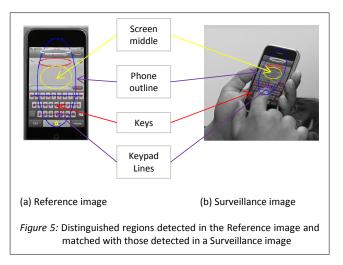
different surveillance videos and SIFT descriptors are invariant to a large degree in terms of changes in scale, intensity as well as viewing angle.

Algorithm 1: Track and Identify the Phone

- **Output:** For every frame in the video, a vector of ellipses that represent the location of the phone as well as location of keys and other such features on the phone in that particular frame
- 1: **detect** MSERs in the reference phone image $I_{REF}(say \{R_{ref}\})$
- select a subset of MSERs in {*R_{ref}*}, which are repeatable across different surveillance scenarios. Let us name this subset *distinguished regions* {*D_{ref}*}.
- 3: for every image I_K in the surveillance video do:
- 4: **detect** MSERs in the image I_K (say $\{R_K\}$).
- 5: **match** regions in $\{R_K\}$ to *distinguished regions* $\{D_{ref}\}$ in the reference image and **select** those regions in $\{R_K\}$ which have high match scores.
- 6: **refine** the output of step 5 by a model-based postprocessing method to finalize the *distinguished regions* $\{D_K\}$

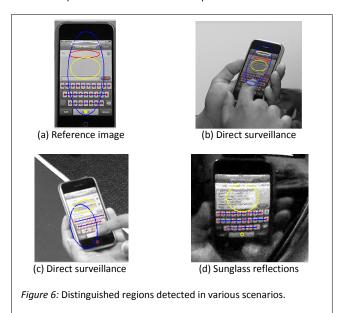
 $\{D_K\}$ contains the {phone location, keys location, keypad lines, ...} in image I_K

We represent the regions returned by the MSER detector as ellipses, and perform affine normalization to turn them into oriented circles before extracting their SIFT descriptors. This pre-processing step makes the matching invariant to affine transformations and hence makes these descriptors robust to a wider difference in viewing angles.



As shown in Figure 5, the *distinguished regions* { D_k } determined in the surveillance image I_k contain answers to questions like "Where is the outline of the entire phone?", "Where is the display screen of the phone?", and "Where are the keys in the keypad of the phone?". From the output of the tracking algorithm, we compute a mask for the entire phone, henceforth called the *phone mask* [Figure 15], which identifies the location of the phone in the image.

Additionally, we have observed that the keys in a QWERTY keypad are arranged in horizontal lines. To take advantage of that structure, we fit lines to the *keys* detected on the phone in the surveillance image. These lines (henceforth referred to as *keypad lines*) help us get a stronger confidence on the location of the keypad of the phone, and that is helpful because the "key pressed" events that we are primarily interested in take place in the keypad area of the phone rather than the entire phone.



We have successfully employed our approach to detect the phone in various surveillance scenarios [Figure 6] including the case in which the video captures a reflection of the typing activity in a person's sunglasses. Once the phone has been identified and located in the video, we now proceed to the next stage in which we would attempt to detect the "key pressed" events in a stabilized stream.

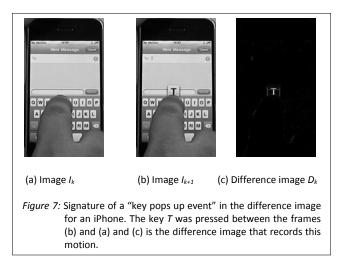
3.3 Change detection by absolute differencing

At the resolution at which our approach is implemented, it is not possible to find out what the user is typing by read it off the display screen on the phone. We had to design an approach which relies on the analysis of the motion of the user's fingers and other events that take place on the phone like the "key pops up" event [Figure 7]. We decided to use one of the simplest yet very powerful methods of motion and change detection, namely, the method of absolute differencing. The general idea of absolute differencing involves looking at the differences between two images of the same scene taken at different times. The parts of the scene that were stationary will look exactly the same in both images, and the differences in the images come from the parts that have moved. Analysis of these differences can determine where in the scene the motion took place as well as what type of motion it was.

We compute a difference image by considering the pixel-wise absolute differences. Let us consider the sequence of images extracted from the video { I_1 , I_2 ... I_M }. Let the absolute difference images between each consecutive pair be the sequence { D_1 , D_2 ... D_{M-1} }, where,

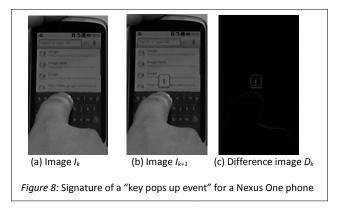
 $D_n(x) = |I_{n+1}(x) - I_n(x)|$, for every pixel x in the images

An analysis of the difference image $D_{\mathcal{K}}$ gives us a good idea of the motion that took place in the scene between the times $t_{\mathcal{K}}$ and $t_{\mathcal{K}+1}$. We begin our analysis by assuming that the phone remains stationary in the video, that is, the user does not move the phone while typing on it. We would later generalize the discussion to involve the movement of the phone as well. We observed that different types of motions or events leave typical signatures in the difference image.



In our experiments, we found out that the motion taking place in the phone area (for a phone with a virtual keypad) can be classified into a very small number of categories:

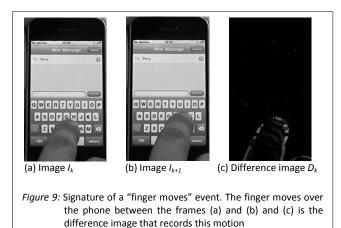
- "Key pops up": This is the event in which a key is pressed by the user. In all virtual keypad phones, whenever a user presses a key (say the letter T [Figure 7]), the letter T pops up on the screen so that the user easily knows what he is typing.
- "Key pops down": This is the event in which the key (say the letter T) that popped up when the user pressed it pops down so that the user can carry on with the typing activity.
- "Finger moves": This is the event in which the user's finger(s) are moving in the phone area between the times when he presses the keys [Figure 9].
- "No movement": This is the event that no movement occurs inside the phone area. This takes place when the user pauses while typing, or just before and after the message has been typed.



Figures 7, 8 and 9 show the difference images for the two most significant events, the "key pops up" and the "finger moves" events

respectively. The signature of the "key pops down" event is very similar to the "key pops up" event.

Thus, the process of detection of the "key pressed" event in the sequence of frames $\{I_1, I_2 \dots I_M\}$ is reduced to the process of detection of the "key pops up" event in the sequence of difference images $\{D_1, D_2 \dots D_{M-1}\}$. We use certain heuristics and parameters to detect the "key pops up" event in the difference image sequence.



3.3.1 Detection of the "key pops up" event

The task of detecting whether a "key pops up" event occurs in a difference image D_k essentially involves searching for a blob-like appearance in the image, This is accomplished by filtering the image D_k with an averaging filter and looking at the places which are local maxima of the filter output. If the filter output at one of these maxima is within a certain range of values (determined empirically), a "key pops up" event occurs in this difference image; otherwise it does not. The following sections A and B explain how certain spatial as well as temporal data in the difference image sequence help us in searching for this event.

Algorithm 2: Detect "key pops up" event in difference image D_K

Output: Set of probable points in D_K where this event occurs Return NULL if no such point is found

1: **filter** D_K with an *averaging filter f*, size(*f*) \propto key_size(D_K)

 $D_{K}' = f * D_{K},$

8:

- 2: calculate D_{K+1} and D_{K-1} as in step 1.
- 2: select a set of local maxima in the filtered output $D_{K'}$. Let us call this set $\{M_{K}\}$.
- 3: for every point (x_K^i, y_K^i) in M_K do:
- 4: **check** if $D_{K}'(x_{K}^{i}, y_{K}^{i})$ is in the proper range.

5: **check** if the ratio
$$\frac{D_{K'}(x_{K}^{i}, \mathbf{y}_{K}^{i})}{D_{K+1'}(x_{K}^{i}, \mathbf{y}_{K}^{i})}$$
 is in proper range.

6: **check** if the ratio
$$\frac{D_{K'}(x_{K}^{i}, y_{K}^{i})}{D_{K-1'}(x_{K}^{i}, y_{K}^{i})}$$
 is in proper range.

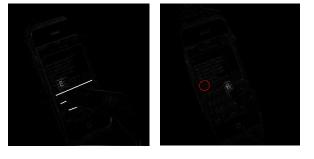
7: **if** (x_K^{i}, y_K^{i}) satisfies all three conditions {4, 5, 6} **then**

add
$$(x_K^i, y_K^i)$$
 to the output.

a) SPATIAL DATA IN THE DIFFERENCE IMAGE

Our tracking algorithm [Section 3.2] gives us information about the location of the phone in the surveillance image as well the location of the keys on the virtual keypad of the phone. Additionally, we also fit *keypad lines* to the detected keys. Figure 10 (a) shows *keypad lines* overlaid on a difference image which has recorded a "key pops up" event. The knowledge of the position of the *keypad lines* and the detected keys helps us know where in the difference image to search for the "key pops up" event.

Our tracking algorithm outputs regions. Hence, apart from the location of the keys and keypad lines, we also have an idea of the size of the keys (in pixels) in a surveillance image. The size of the keys is approximated as the average size of the regions which are reported as keys by the tracking algorithm. The knowledge of key size helps us to determine the size of the averaging filter that we use while searching for the "key pops up" event (Figure 10 (b)). For accurate detection, it is very crucial to have an averaging filter that matches the size of the key that pops up in the difference image.



(a) Keypad lines

(b) Size of the averaging filter

Figure 10: Spatial data helps in searching for "key pops up" event

- (a) Keypad lines overlaid on a difference image which records the pressing of the key *E*. Keypad lines give us a good idea of where to look for a "key pops up" event.
- (b) The size of the averaging filter is important for detecting the type of blob that identifies a "key pops up event". The size of the red circle (the averaging filter) must match the size of the key (in this figure, letter *H*) that pops up.

b) TEMPORAL DATA IN THE DIFFERENCE IMAGE SEQUENCE

In order to capture all the key pressed events, we extract frames from the surveillance video at a rate of 30 frames per second. Surveys of typing speeds ([7], [8]) show that the average typing speed in virtual QWERTY keypads (like the ones on the phones we experiment on) ranges around 15-30 words per minute. This means that in a video of 30 seconds (900 frames) the user typically types only about 40 to 80 keys. Our job is to find those 40 to 80 difference images out of 900, in which a "key pressed" event was recorded. In the rest of the 820 to 860 frames, the difference image mostly records a "finger moves" event (Figure 9). Hence our algorithm must be able to correctly reject the "finger moves" events in a robust and accurate way. Analysis of temporal relations in the difference image sequence helps us differentiate between "key pops up" events and "finger moves" events and thus reject these "finger moves" events. Algorithm 2 gives a detailed outline of our method.

Figure 11 shows three successive frames that record "finger moves" events. The moving of the finger over the phone is a continuous event and hence is detected in many of the difference images in the sequence.

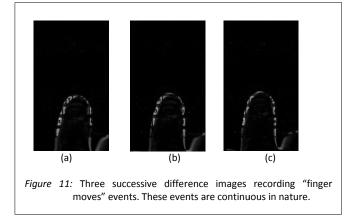
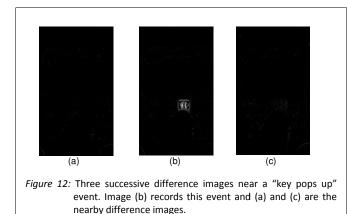


Figure 12 shows three successive frames near a "key pops up" event. The 'key pops up' and 'key pops down' events are sporadic or episodic in nature. The key pops up in an instant, stays on for some time (during which the difference image shows a zero difference at the place where the key pops us) and then pops down in an instant.



Thus, by examining the neighboring images in the difference image sequence, we are able to reject "finger moves" events and obtain a higher confidence over the prediction of a "key pops up" event. The process involves comparing the ratio of pixel values (after averaging filter) in the blocks that represent the particular event in the difference image D_K with the pixel values at the same locations in its time neighbors D_{K-1} .

3.3.2 "Which key was pressed?"

Once a "key pops up" event has been recorded in a difference image D_{K} , our task now is to predict which key was pressed. While template matching with the appearance of the key (in the difference D_{K} image or the image I_{K+1}) seemed to be a promising idea initially, as we started lowering the resolution of the images (for video surveillance from a distance or for surveillance on the reflections on a sunglasses etc.), it was difficult to distinguish the keys from each other based solely on their appearance. The scenario is shown in the Figure 13, which shows images from two surveillance videos that have captured the typing activity at a rather low resolution. In 13(a), the key *R* was pressed but template matching would give positive results for many letters that look like R at that resolution (for example B, P, E, H, A). We decided that the best way to predict which key was pressed was to look at the location of the blob that was detected in the difference image while searching for the "key pops up" event.

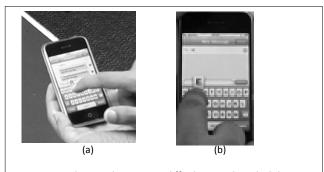


Figure 13: At low resolutions, it is difficult to predict which key was pressed based on its appearance. So template matching fails

Algorithm 3: Detect which key was pressed at the time t_K

- **Input:** i) The point (x_k, y_k) in the difference image D_k , where a "key pops up" event has occurred.
 - ii) A keypad map for this phone that says where on the phone screen a key pops up when that particular key is pressed by the user.
- **Output:** Set of probable letters that were pressed along with respective probabilities. Return NULL if no key was pressed at time t_k .
- 1: **estimate** a homography H_K between the image I_K and the reference image I_{REF} (details in Algorithm 4).
- 2: warp the difference image D_K by the transformation H_K to get $D_K' = D_K * H_K$

 (x_K, y_K) transforms to (x_K', y_K') under this transformation

- 2: **perform** posterior optimization via the steps 3 and 4. (explained further in the Section 3.3.2)
- 3: for every key *i* in the keypad do:

4:
$$p'(i) = \frac{a_{intersection}}{a_i}$$

 $p'(i) \propto$ probability that key *i* was pressed

 a_i = area where key *i* pops up if it is pressed

 $a_{intersection}$ = area of overlap between the blob at (x_{K}', y_{K}') in D_{K}' and the area where key *i* pops up if pressed

- 6: **return** NULL **if** *a*_{intersection} = 0 for all keys
- 5: **select** the *n* keys with the highest probabilities
- 7: **renormalize** the probabilities to make them sum to 1 and **output** all the *n* (key, probability) pairs.

Algorithm 3 gives an outline of our approach. We begin by computing the transformation that warps the surveillance image I_{K} to the reference image I_{REF} (details in Algorithm 4). We warp the

difference image D_{κ} by the same transformation to obtain a warped difference image $D_{\kappa'}$. We then perform posterior optimization to determine which keys have the highest probabilities of being pressed, given the warped difference image $D_{\kappa'}$ and the point ($x_{\kappa'}$, $y_{\kappa'}$) where the "key pops up" blob occurs. At this stage, we take advantage of the fact that it is easy to obtain from a single experiment, a map that says which region of the screen pops up when a particular key is pressed on this phone.

For any key *i* in the keypad,

$$p(i/D_K') \propto p(D'_K/i) * p(i) \tag{1}$$

where, p(i) = prior probability of the key *i* being pressed

- $p(i/D_{K}')$ = posterior probability of the key *i* being pressed given D_{K}' and (x_{K}', y_{K}')
- $p(D'_{K}/i) =$ probability the blob at $(x_{K'}, y_{K'})$ in $D_{K'}$ given that key *i* has been pressed
 - $=\frac{a_{intersection}}{a_i}$
- a_i = area where key *i* pops up if it is pressed (given by the map)
- $a_{intersection}$ = area of overlap between the blob at ($x_{K'}$, $y_{K'}$) in $D_{K'}$ and the area where key *i* pops up if pressed

Based on formula (1) above, we compute the posterior probabilities of keys by computing the ratio of areas of overlap. If there is no overlap at all between the blob in the difference image and the "pop up" areas of the keys in the given map, we assume that no key was pressed in this frame.

From the results of the posterior optimization, we could either choose to output the one particular key with the highest probability as the one being pressed or we could output a list of probable keys and their corresponding probabilities. An example output of this stage might look like "There is a 70% chance that an E was pressed, and a 30% chance that it might have been an R". We are exploring ways to utilize these probabilities by designing a probabilistic text processing method to refine the results of our overall approach.

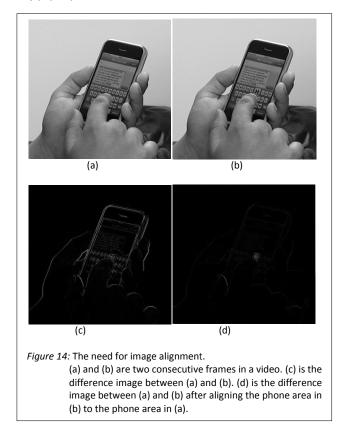
3.4 Image Alignment

Image alignment is one of the most crucial parts of our entire approach. The analysis in Section 3.3 of this paper assumes that the phone is stationary and all the events and motions are with respect to the phone. In a general scenario, while typing, the user moves the phone as well. In this case, the difference image D_K between two consecutive frames in the video I_K and I_{K+1} contains information about:

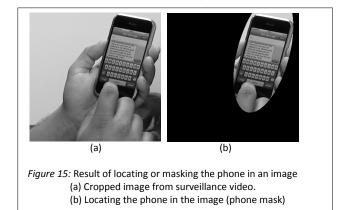
- The overall motion of the phone and the hand(s) holding the phone
- The motion of the fingers in the phone area and the "key pressed events"

The first type of motion is a distraction for us as we are only interested in the motion that happens in the phone area. Figure 14 shows two consecutive images (a) and (b) (let us call them I_a and I_b) in the image sequence of a surveillance video. A "key pressed event" occurs between the times t_a and t_b in the video. (c) is the

difference image between I_a and I_b calculated by taking the pixelwise differences in both images. We can clearly see the disturbance in the difference image caused by the slight movement of the phone. In fact, detecting the "key pops up" event in the difference image (c) is very difficult. (d) is the difference image computed between images I_a and I_b ', where I_b ' is the image I_b subjected to a transformation that aligns the phone area in image I_b to the phone area in image I_a . It is evident that the difference image (d) is more meaningful for our analysis and also clearly shows the "key pops up" event in it.



Our tracking algorithm [Section 3.2] tells us the location of the phone in the image and also returns the region that is occupied by the phone in the image. From the output of this stage, a *phone mask* is computed so that we mask out everything else in the surveillance image except the phone, and focus on the object of interest. The *phone mask* [Figure 15] plays an important role in the image alignment process as this helps us find features that lie exactly on the phone.



One of the initial ideas that we explored was to align the phone in all the images in the surveillance video to the reference image of the phone. This approach, while it seems to simplify the process a lot, turned out to be a failure because of several reasons. One apparent reason was that in many of the surveillance images, a large part of the phone in occluded by the user's hands; so there weren't enough correct correspondences to estimate a correct transformation that warps the surveillance image to the reference image. Another reason was that our method of absolute differencing relies on the temporal relations between the video frames. Hence, separately aligning each of the frames to the reference image destroyed that temporal relation between successive frames.

In our approach, before computing the difference image between two successive images I_{κ} and $I_{\kappa+1}$, we align the phone areas in the two images via SIFT matching. The very reason that we use only features that lie on the phone makes sure that the warping between these images stabilizes the phone area (so that the difference images do not show the movement of the phone).

An important requirement of image alignment occurs at the stage where we determine which key was pressed by the user, once a "key pops up" event has been detected. The first step in Algorithm 3 is to align the surveillance image I_{K} to the reference image I_{REF} by a homography H_{K} . Computing this homography turns out to be a challenging task as the user's fingers obstruct a large part of the phone's keypad in a "key pressed" frame. These occlusions, coupled with wide differences in illumination and viewing angle often lead to incorrect homographies being computed between the I_{K} and I_{REF} . Algorithm 4 describes the method of alignment that we designed to overcome this challenge.

Algorithm 4: Align "key pressed" frame I_K to the reference image I_{REF}

Output: A homography H_K that warps I_K to I_{REF}

- 1: find a clear frame I_{CF} , in the image sequence of the same video, such that I_{CF} has an unobstructed view of the phone keypad.
- 2: estimate homography H_{CF-REF} between I_{CF} and I_{REF} .
- 3: estimate homography H_{K-CF} between I_K and I_{CF} .
- 4: **calculate** the homography H_K by:
 - $H_K = H_{K-CF} * H_{CF-REF}$

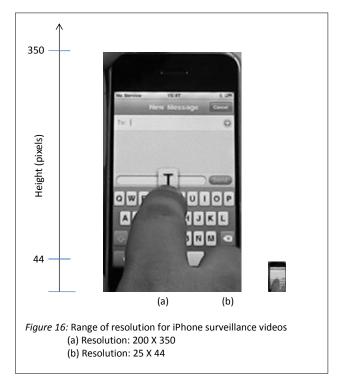
Instead of directly aligning the image $I_{\mathcal{K}}$ (called the target frame) to I_{REF} , we first choose an image I_{CF} (called the clear frame) in the same video that has an unobstructed view of the phone keypad. To find this image, we again use the output of our tracking method (Section 3.2) which also returns the number of keys detected in each surveillance image in the video. If more number of keys were detected, that image has a more unobstructed view of the keypad. We then compute a homography between the reference image and the clear frame. This homography would be accurate because we have an unobstructed view of the keypad and hence there would be reliable feature matches between the two images. The next step is to estimate a homography between the target frame and the clear frame. This homography would also be correct as both images are from the same video and have roughly the same lighting conditions and viewing angles. The final homography that we require is just a multiplication of the two homographies just computed.

4 RESULTS

For our experiments, we used a Canon Vixia HG 21 Camcorder (costs about 1000 USD). The experiments were conducted in an indoor environment, and the camera was at a distance of 2 to 3 meters from the user.

4.1 Direct surveillance with no phone movement

We conducted our first set of experiments keeping the phone stable (hence not moving) while the user types on it. The experiments were performed on a direct surveillance setup where the camera had an unobstructed view of the phone and was at a distance of about 2 meters from the user. The results we obtained for these surveillance videos were excellent and showed promise that our algorithm was ready to be applied to more challenging scenarios.



4.1.1 iPhone dataset

For this dataset, we conducted the experiments at four different resolutions of the surveillance video. The Figure 16 shows frames at the highest and lowest resolution videos. Table 1 below summarizes the results of this set of experiments. *Ground truth* refers to the string that was typed by the user and *Reconstructed string* is the string predicted by our algorithm. It can be observed that we predicted the string with 100% accuracy at resolutions which were at and above 50X88 pixels.

Ground truth: the quick fox jumped over lazy dog

Exp 1.1, 1.2 and 1.3: Video resolution: 200 X 350, 100 X 175, 50 X 88

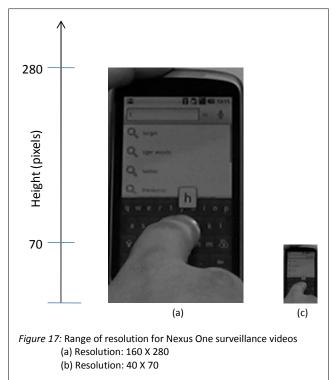
Reconstructed string: the quick fox jumped over lazy dog

Exp 1.4: Video resolution: 25 X 44

Reconstructed string: the quick fox jumpedxlovder nlazy dog

Table 1: Results of experiments for the iPhone dataset

In the case Exp 1.4, in which the input video had a resolution of 25X44 pixels [Figure 16(b)], our algorithm still predicted most parts of the string correctly. In terms of the number of frames that fired as "key pressed events", there is a false positive rate of 11 % and no false negatives. The *Levenshtein Edit Distance* between the *Reconstructed string* and the *Ground truth* is 5 characters. Based on this measure, there is an error rate of 14% per character for Exp 1.4. Another popular measure used for evaluation of Machine Translation is *Word Error Rate (WER)*, which is based on the normalized Levenshtein edit distance between the hypothesis and the reference, assuming a word as the basic unit of comparison. The *WER* in case of Exp 1.4 turns out to be (2/7). It is interesting to note that at the resolution at which Exp 1.4 was recorded [Figure 16(b)], it is not possible for a human being to predict the user-typed string by watching the video.



4.1.2 Nexus One dataset

We conducted a similar set of experiments on surveillance videos of the Nexus One phone. The experiments were in three different resolutions of the surveillance video. Figure 17 shows frames extracted from the video. Table 2 summarizes the results of the experiments.

In these experiments, we were also able to detect when the user switches the keypad from "ABC" mode (in which the letters appear on the virtual keypad) to the "123" mode (in which numbers keypad replaces the alphabets keypad at the same place on the virtual keypad) and the "Symbols" mode (in which the symbols keypad replaces the alphabet keypad on the phone). Based on simple heuristics, we also recovered when the user types in the "lower case" and "upper case". These features can be very useful in scenarios where the goal is to recover passwords and other such information where the string to be recovered is case-sensitive and is likely to contain special characters.

Ground truth:

the quick fox jumps over the lazy dog BROWN DOG. tHHE QUICK BROWN FOX JUMPS OVER THE LAZY DOG. 9876501234@#\$%&*+()

Exp 2.1: Video resolution: 160 X 280

Reconstructed string:

the qick fox jumps over the lazy dog BROWN DG. tHHE QUICK BROWN FOX JUMPS OVER THE LAZY DOG. 9876501234@#\$%&*+()

Exp 2.2: Video resolution: 80 X 140

Reconstructed string: the quick fox jumps over the lazy dog BRWN DOG. tHHE QUICK BROWN FOX JUMPS OVER THE LAZY DOG. 9876501234@#\$%&*+()

Exp 2.3: Video resolution: 40 X 70

Reconstructed string: the qick fox jumps over the lazy dog BROWN DOG. tHHE QUICK BROWN FOX JUMPS OVER THE LAZY DOG. 9876501234@#\$%&*+()

Table 2: Results of experiments for the Nexus One dataset

It can be observed that we predicted the string with almost complete accuracy at all resolutions. In terms of the number of frames that fired as "key pressed events", there is a false negative rate of 1.05 % and no false positives. The *Levenshtein Edit Distance* between the *Reconstructed string* and the *Ground truth* is 1 character in all the three cases; there is an error rate of 1 % per character according to this measure. The Word Error Rate in all the cases is (1/20) in all the three cases; we got one incorrect word in the entire string in the three cases.

4.2 Direct surveillance with phone movement

In this set of experiments, the user types on the phone and the phone is allowed to move (in contrast to the scenario in Section 4.1 where the phone remains static). This case is challenging because we have to deal with the movement of the phone as well as the

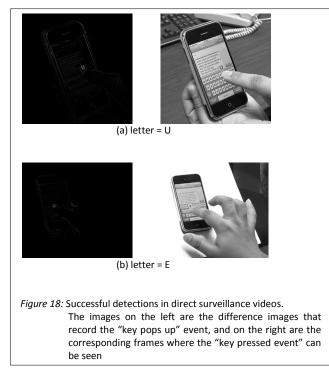
Ground truth: the quick fox jumped over the lazy dog

Reconstructed string: thevvb qcuikm fnooxajlummed doverb thv azztm dcvog

Table 3: Results of reconstruction for direct surveillance with phone movement

movement of the user's fingers in the phone area.

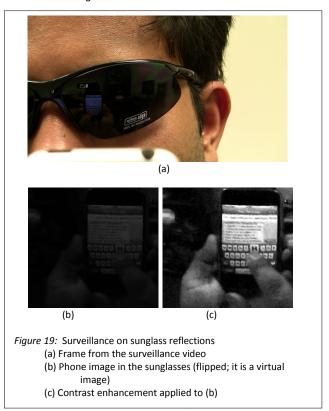
Table 3 shows the results of our algorithm on one surveillance video. The bold letters in the reconstructed string are the correctly detected letters. There is a rather large quantity of false positive "key pressed events", around 50%, because of which the output string does not make any sense. The number of false negatives is around 10%. The Levenshtein Edit Distance between the Ground truth and Reconstructed string is 19 characters, which is also pretty large considering that the length of the input string is only 29 characters. However, in terms of the number of characters in the Ground truth that were recovered in their correct relative order in the Reconstructed string, we have an accuracy of 90 %, that is, 26 out of the 29 characters typed by the user have been detected in their correct order by the algorithm. A number of false positives can be reduced by manipulating the parameters of our change detection algorithm. A language model based post-processing step would be very helpful in predicting the user-typed string with higher accuracy. In the keyboard surveillance method proposed by Balzarotti et al [4], a major part of their approach is language modeling and text analysis to reproduce what was being typed on the keyboard.



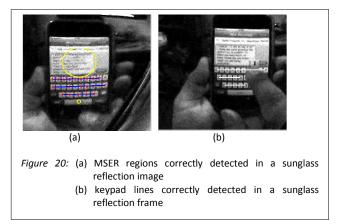
For each "key pressed" event, instead of storing just one character (for example, the user has pressed the letter E), we store many probable characters with their respective probabilities (for example, there is a 55% chance that an *E* has been pressed, but a 45% chance that it might actually have been an *R*; the letters *E* and *R* are next to each other in the phone keypad). The process of obtaining these probabilities is explained in Section 3.1.2 [Algorithm 3]. The reconstructed string shown in Table 3 shows only the most probable outputs for each letter. We are in the process of exploring ways to use these probabilities meaningfully to produce a correct output string.

4.3 Surveillance on the reflection on sunglasses

We extended our approach for automatic text reconstruction to a surveillance video of the reflection of a user's typing activity in his sunglasses. The threat scenario is the one shown in Figure 19. We applied our algorithm to a surveillance video of sunglass reflections and obtained very encouraging results. The SIFT+MSER tracker [Section 3.2] performed remarkably well on this video. Some results can be seen in Figure 20.



Some correctly detected "key pressed frames" are shown in Figure 21. In terms of correctly detecting the "key pressed events", we have several correct detections (25 to 50%) in sunglass reflection videos. However, there are still a lot of false negatives as well as false positives that result in the output strings not being meaningful.



One of the primary reasons is a failure in the image alignment process [Section 3.4, Algorithm 4] that is required to determine "which key was pressed". Misalignments occur primarily because the sunglass reflection images are noisy, they have a large change in illumination from the reference image I_{REF} , and have radial distortion (they are images on a spherical mirror, the sunglass). One particular case of misalignment is shown in Figure 22.

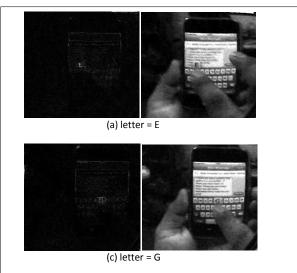
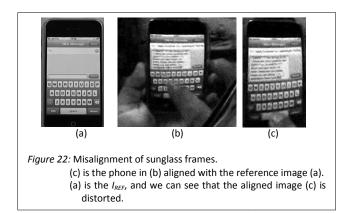


Figure 21: Correct detection of keys pressed in sunglass reflection video. The images on the left are the difference images that record the "key pops up" event, and on the right are the corresponding frames where the "key pressed event" can be seen.



5 How REAL IS THE THREAT? (PRACTICAL LIMITS)

In Appendix – I [Section 8] we provide a discussion on the relevant parameters if this threat was to be planned in a real scenario. The following is a discussion based on the results of that analysis.

5.1 How good are current equipments

In Section 8, we saw that the maximum resolution with which a particular object can be captured by a camera depends upon

- The diameter of its lens
- Distance of object from the camera

For our algorithm, we have demonstrated successful results even at an object resolution 25 X 44 (pixels in each dimension) (for the iPhone). This was in the case when the phone was static, but in the general cases we have promising results with resolutions around 100 X 175.

By the expression (3) [Section 8.2.1], the minimum diameter of a lens required to directly capture the typing activity of the phone at the resolution of 100 X 175 from a distance of 1 meter is 1.16 mm.

The diameter of most good cell phone cameras (iPhone, Nexus One etc.) is in the range of 1.3 to 1.5 mm. This implies that if Alice

is at a distance of around 1 m from Bob, and has an unobstructed view of Bob's phone she can get an automated transcript of what Bob is typing by recording a video from her own cell phone itself. This can very easily take place in a crowded place like a bus or a metro train.

The diameter of most cheap digital cameras (under 200 USD) ranges from 2.0 to 6.0 mm; they can effectively spy from a distance of 1 to 4 meters from the typing user. The diameter of slightly high price range (under 500 USD) digital cameras ranges up to 20 mm; they can be used to spy upon the person up to distances of 10 m or more.



Figure 23 and Figure 24 provide an approximate range at which direct and indirect surveillance can be carried out using our algorithm with the use of different types of cameras. Thus, overhead surveillance cameras and such equipments can easily directly spy on the phone user whereas high quality cameras and telescopes would be required to spy on the reflection on glasses or eye from distances of 5 m or more. The analysis above predicts that the threat that we examine is real and could be carried out using moderately priced equipment in a real life setting.



6 CONCLUSION

Through our current work, we have shown that automatic text reconstruction solely from a surveillance video is possible for eavesdropping on a smart phone. We have developed a method for tracking and identifying a phone that has been successful in a wide range of surveillance videos. This algorithm has performed remarkably well even when we applied it for tracking the phone in a video that captured a reflection of the phone in the user's sunglasses. Based on an analysis of optical parameters and optical equipments, we have predicted that automatic spying on a phone user is a potential threat that could be carried out with readily available cameras using state-of-the-art computer vision algorithms.

There are several possible directions in which future work could be carried out in this area. For further improvement of our spying algorithm, the use of a good language analysis model would be very helpful. It is also necessary to conduct more experiments in real world settings to get a better idea of the usability of the approach. There lies another vast area of designing methods for prevention of this threat. There have been reports of breach privacy filters installed on touch screens [19]. There are also new types of phone touch screens, which instead of providing visual feedback (in the form of the character "popping out") provide tactile feedback to the user in the form of a mechanical click [20] or a vibration [21] under the user's fingertips when she presses a key in the virtual keypad. There are also new technologies which provide for alternative ways of text input on a phone touchscreen rather than typing on it [22].

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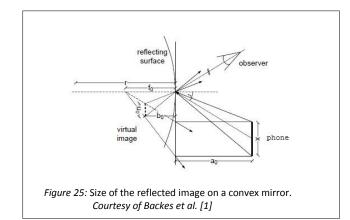
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8 APPENDIX – I: AN OPTICS PRIMER

In this section we present an analysis of the relevant parameters of an optical system that are required to carry out the threat scenario that we imagine in the real world. Backes et al [1] have provided a very clear explanation of these parameters.

8.1 Size of the object of surveillance

The first question that matters to us is "What is the size of the object that we want to capture in the video?". In the case of direct surveillance it is the size of the phone. In case of surveillance that involves capturing the typing activity from a reflection in the person's glasses or his eyeballs, the question is "What is the size of the phone's image in the reflecting surface?" For answering these questions we need to refer to some of the basic optics theories.



8.1.1 Size of the reflected image

The reflection of an object in a curved mirror creates a virtual image that is located behind the reflecting surface. The overall situation is depicted in Figure 25. If the width of a spherical mirror is small compared to its radius, it is common to approximate the mirror as a lens of focal length $f_0 = r/2$. The location b_0 of the virtual image (the distance between the virtual image and the reflecting surface), given the location a_0 of the object is given by the *thin lens equation* as, $b_0 = 1/(2/r - 1/a_0)$

The size u_0 of the virtual image is given by $u_0 = b_0 x / a_0$, where x is the size of the phone. Finally we have to consider that the image appears smaller if seen from an angle ; the apparent size $u_1 = u_0 \cos \gamma$.

The size of the iPhone is 11.5 cm X 6.2 cm. Using the formulae derived above, assuming that a person holds the phone at a distance of 30 cm from his eyes while typing, the size of the image of the iPhone in a normal pair of sunglasses (assuming a radius of curvature of 200 mm) is 1.07 cm X 0.57 cm, and the size of the image of the iPhone in a person's eye balls (assuming the average eye ball radius of 8mm) is 1.6 mm X 0.86 mm. Thus, calculations

reveal that the image of the phone in a person's glasses is about a tenth of the actual size, and the size of the image of the phone in his eyes is about a hundredth of the actual size.

8.2 Limits of optical resolution

Some relevant questions are, "Is it feasible to conduct the video surveillance on another phone by using the camera in my phone?", "How powerful a camera do I need to make the automatic detection work on the reflection of the typing activity in another person's sunglasses or eyes?". For answering all these questions, we first need to understand the term "Optical resolution".

Let the distance from the camera to the object being captured be d. The object might be the phone or its reflection on some surface. Let n be the required resolution of this object on the camera image (in pixels). If the size of the object is u_1 , then the optical resolution α (in radians) required to capture the object with the desired resolution in the image is given by,

$$\alpha = \arctan(u_1/nd) \approx u_1/nd \tag{1}$$

where the approximation holds as $u_1 \ll d$.

8.2.1 Diffraction Bounds

Diffraction is a physical phenomenon that diffuses light or any other electromagnetic wave, whenever it passes some aperture. Though this phenomenon is well-known for being visible to the human eye for very small apertures, in case of high magnifications, it is noticeable even for large apertures like lenses used in cameras and telescopes. In fact, as we will see further in this discussion, diffraction constitutes one of the most limiting parameters in the use of cameras for surveillance scenarios.

The influence of diffraction on the maximum optical resolution of a telescope is given by *Rayleigh's criterion*. Let two point sources P1, P2 be given such that the angle between these two sources is α (in radians). Let D be the diameter of the lens of the camera and λ the wavelength of the light. Then Raleigh's criterion states that the two points P1, P2 can be distinguished if and only if

$$\alpha \ge 1.22 \,\lambda/D \tag{2}$$

From equations (1) and (2), we can derive an expression for the maximum resolution of an object that can be captured by a camera lens at a given distance. The expression is:

$$n \le u_1 D/(1.22 \lambda d) \tag{3}$$

From the expression above, it is apparent that the maximum resolution that can be captured by a camera or telescope lens is directly proportional to the diameter of the lens, and inversely proportional to the distance between the camera and the object.